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# A Routing Algorithm for Wireless Ad Hoc Networks with Unidirectional Links

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**Abstract.** Most of the routing algorithms for ad hoc networks assume that all wireless links are bidirectional. In reality, some links may be unidirectional. In this paper we show that the presence of such links can jeopardize the performance of the existing distance vector routing algorithms. We also present modifications to distance vector based routing algorithms to make them work in ad hoc networks with unidirectional links. For a network of $n$ nodes, neighbors exchange $n \times n$ matrices to propagate routing information. This results in loop-free routes.

**Keywords:** mobile ad hoc networks, routing, unidirectional links, distance-vector routing

## 1. Introduction

The mobility pattern of the nodes in an ad hoc network is often non-deterministic. Hence, the network topology is always in a flux. There has been a significant amount of effort towards developing routing algorithms for such networks. These algorithms can be classified into (a) *cluster-based* algorithms, and (b) *flat* algorithms. In cluster-based algorithms [1–4], at regular intervals, a subset of nodes is elected as *cluster-heads*. A node is either a cluster-head or one wireless hop away from a cluster-head. Nodes that are not cluster-heads will, henceforth, be referred to as *ordinary* nodes. When an ordinary node has to send a packet, the node can send the packet to the cluster-head which routes that packet towards the destination. In flat routing algorithms [5,8–11] each node maintains routing information.

These routing algorithms have contributed significantly towards the understanding of the problem and the feasible solution approaches. However, to successfully deploy ad hoc networks we need to understand the various ways in which RF-propagation characteristics can impact the routing problem. Several models based on the IEEE 802.11 physical and medium-access control layer protocol [6] have used its *Request_to_Send* (RTS) and *Clear_to_Send* (CTS) control message exchange option to avoid collision and facilitate communication over bidirectional links. We will concentrate on a scenario that has not been considered in these models, namely presence of some *unidirectional links* in the network.

Some links may be unidirectional due to the *hidden terminal problem* [12] or due to disparity between the transmission power levels of the nodes at either ends of the link. Almost all existing routing algorithms tend to assume that all links are bidirectional. *In this paper we intend to evaluate the impact of unidirectional links on some of the existing distance vector based routing algorithms for ad hoc networks.* Based on the understanding of the impact of such links, we propose a strategy to modify existing distance-vector based algorithms so that they can work correctly in an ad hoc network that has a combination of unidirectional and bidirectional links. Evaluation of the impact of unidirectional links on hierarchical cluster-based routing algorithms and link-state routing algorithms is slated for future research.

Section 2 describes two scenarios in which unidirectional links may arise. Section 3 presents a brief description of some of the existing flat routing algorithms. As the focus of this paper is on such algorithms, we do not describe the hierarchical algorithms. In section 4 we discuss the impact of unidirectional links on some of the existing flat routing algorithms for ad hoc networks. In section 5 we prove that exchanging $O(n)$ size messages, as performed in existing distance vector based routing algorithms that assume all links to be bidirectional, is not sufficient. We also propose an extension to such routing algorithms in which adjacent nodes exchange $O(n^2)$ size messages. This is a significant increase in the communication overheads. Future work will be focused on reducing this overhead. MAC sub-layer issues pertaining to routing with unidirectional links are discussed in section 6. Finally, we present the conclusions in section 7.

## 2. Unidirectional link scenarios

Some node, say $A$, may be able to receive messages from node $B$ as there may be very little interference in $A$'s vicinity. However, $B$ may be in the vicinity of an interfering node and, therefore, be unable to clearly receive $A$'s messages. If all data communication is preceded by a two-way handshake between nodes (like RTS-CTS) then neither will exchange data packets with the other over this link. However, if such a handshake is not used at the MAC sub-layer, node $B$ may be able to send data packets to node $A$. So, the link between $A$ and $B$ is directed from $B$ to $A$. Of course, what happens if $B$ expects MAC sub-layer acknowledgements from $A$ but can-

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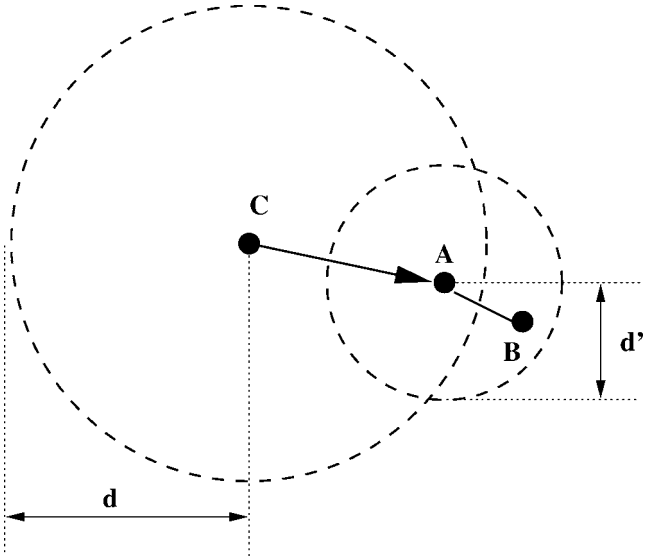


Figure 1. Presence of unidirectional links due to energy depletion.

not receive them due to interference? We will discuss this issue later in section 6.

The other scenario for unidirectional links has to do with batter life. Sometimes nodes may choose to have unidirectional links incident on them in order to conserve energy. For example, let the maximum power-level at which nodes can transmit, when they have a sufficient energy supply, be $p$ watts. This enables their transmission to reach nodes up to $d$ distance units away. However, when a node's energy supply is depleted it may choose to lower its maximum transmission power to $p'$ watts. As a result its range may reduce to $d'$. The consequence is depicted in figure 1. Node $A$'s energy supply is depleted, but nodes $B$ and $C$ still have sufficient energy. So, while $A$ can receive transmissions of $B$ and $C$, only $B$ can receive $A$'s transmissions. This yields a bidirectional link between $A$ and $B$ and a unidirectional link from $C$ to $A$.

By reducing its energy consumption $A$ can stay operational for a longer period of time and provide potentially improved network connectivity. For example, in figure 1, $A$ can continue to provide a two-hop path from $C$ to $B$. Had $A$ dropped out of the network, $B$ would have been unreachable from $C$.

So, link unidirectionality may be a *persistent* phenomenon, especially if some nodes experience: (i) a significant depletion of their energy supply, or (ii) a persistent and strong interferer. Alternatively, unidirectionality may be a *transient* phenomenon where a link quickly transitions from unidirectional to bidirectional state. The frequency of such transitions, and the duration of stay in each state would be a function of offered traffic, terrain, mobility pattern, and energy availability.

## 3. Previous work

The *Destination Sequenced Distance Vector* (DSDV) [11] approach is a modification of the distance vector routing algorithm used earlier in ARPANET. In DSDV, each node maintains a distance vector that contains entries for each destination. The entry indicates the distance estimate and the next hop to be taken by a packet to reach a destination. Each entry has a sequence number associated with it, indicating its *freshness*. If a destination is unreachable, the distance metric is set to infinity. Periodically a node's distance estimates are diffused to neighbors. When a node $p$ loses a link that it was using to forward packets meant for destination $q$, $p$ sets its distance metric for $q$ to infinity and propagates this information with a higher sequence number. Such updates are diffused immediately, without waiting for the next update time. Similarly, when a path is found to a hitherto unreachable node the finite distance metric to that destination is propagated immediately through the network.

*Dynamic Source Routing* (DSR) [8] uses a diffusion based mechanism to find a route to the destination. Instead of periodically exchanging routing information between nodes, route(s) are discovered when a node has to send packets to some destination node. During this process intermediate nodes can use the discovered routes to update their own routing information. Caching of recently discovered routing information is employed to speed up the routing process. The route maintenance mechanism does the following: (i) sends a *route error* packet to the source if it detects that the route to the destination is broken, and (ii) either tries to use any other cached route to the destination or invokes route discovery once again. In order to route packets, the source completely specifies the path the data packet should take. This can significantly increase the communication overheads, especially as the network diameter increases.

In the *Ad hoc On-demand Distance Vector* (AODV) scheme [10], route discovery and maintenance are performed on demand, as in DSR, along with hop-based routing as in DSDV. In order to reduce communication overheads, as compared to DSDV, updates are propagated only along *active* routes, i.e., routes that have seen some traffic in the recent past.

The *Temporally Ordered Routing Algorithm* (TORA) [9] is based on the notion of edge-reversal [5]. One instance of the algorithm is executed for each destination and a directed graph is maintained with respect to each destination. Only bidirectional links are considered, and a direction is associate with each link. Directed paths between every pair of nodes are initially determined through a sequence of edge reversals. When any node detects that it has lost the path to a destination (all edges incident on the node are directed towards it, in the graph for that destination) it performs full edge reversal so that it has only outgoing links to all its neighbors, and initiates route rediscovery for that destination. If a network partition is detected, the source is informed about the same.

We have not discussed cluster-based routing algorithms as this is not within the scope of this paper.

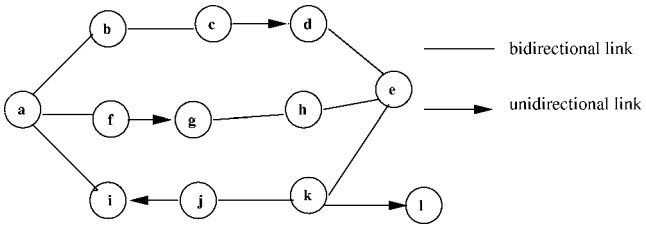


Figure 2. Ad hoc network with unidirectional and bidirectional links.

## 4. Problem description

Several flat routing protocols [9–11] and hierarchical routing protocols [1–4] assume that all wireless links are bidirectional.[1] In the presence of unidirectional links several problems arise for distance vector based algorithms. For the purpose of illustration, let us consider DSDV [11]. AODV [10] has similar behavior. Other flat routing protocols may also exhibit similar problems.

Let us consider three interesting phenomena, illustrated with the help of the network configuration shown in figure 2.

1. *Knowledge asymmetry.* There is a two-hop path from $j$ to $a$: $jia$. However, due to link $\vec{ji}$ being unidirectional, $i$ cannot directly inform $j$ about the path. *Just because i knows that j is its neighbor, i cannot assume that j also knows that i is its neighbor.* Simple diffusion strategy may not be sufficient to propagate information about network topology.

2. *Routing asymmetry.* In AODV, during the path discovery phase, let an intermediate node, $v_i$, get to know that the shortest path from $x$ to $y$ is $xv_1v_2 \ldots v_{i-1}v_iv_{i+1} \ldots y$. Then, $v_i$ concludes that the shortest path from itself to $x$ is $v_iv_{i-1} \ldots v_1x$: the lexicographical reversal of the path prefix ending at $v_i$. However, if there exists a unidirectional link on the path from $x$ to $v_i$, then $v_i$'s conclusion would be wrong. In figure 2, as the link $\vec{ji}$ is unidirectional, the shortest path from $i$ to $j$ consists of seven hops and the path from $j$ to $i$ consists of one hop: *a routing asymmetry*.

3. *Sink unreachability.* In DSDV path updates are initiated by the destination node. In AODV a source node finds a route to the destination only when a sequence of *route replies* flows back on the path from the destination to the source. In figure 2, there exists a path to node $l$. So, it could be the destination of packets. However, there is no way node $l$ can inform $k$ that the latter can reach the former in one hop. So, reachability information about $l$ cannot propagate to other nodes. Node $l$ is a *sink* node as all its incident links are directed towards it. *The network topology may indicate that a sink is reachable from other nodes. But due to the limitations of the routing algorithm no node knows of the existence of the sink, making it effectively unreachable.* Even if nodes knew of the existence of a sink, unicast packet routing protocols sitting on top of MAC sub-layer protocols that require acknowledgements could not use the link incident on the sink. However, for a variety of broadcast and multicast protocols where MAC sub-layer acknowledgements are not expected the sink can be a recipient of packets.

In fact, the problem with DSDV and AODV in the scenario shown in figure 2 is quite serious. As they can only use bidirectional links for routing purposes, they will ignore links $\vec{cd}$, $\vec{fg}$, $\vec{ji}$, and $\vec{kl}$. As a result, even though nodes $a$ and $e$ are reachable from each other, DSDV and AODV will perceive $a$ and $c$ to be in different network partitions.

In DSR, let $i$ receive a path discovery message from $j$ along $\vec{ji}$. When $i$ has to send an acknowledgement to $j$ it may need to initiate a new path discovery to find a route to $j$. The acknowledgement should then be sent along this route. Thus, while DSR does not ignore the possibility of unidirectional links, it makes an implicit assumption that routes in both directions always exist between a pair of nodes. In the proposed algorithm we make a similar assumption.[2] The basic difference between DSR and the proposed protocol is the following: DSR pays a high price for each data packet because such packets have to carry information about the entire route. The proposed protocol avoids paying such a price per data packet, but incurs higher route discovery and maintenance costs. Thus, while DSR would be especially suitable for high mobility, low data traffic networks, the proposed protocol would be suitable for low mobility, high data traffic networks.[3]

## 5. Solution approach

Each node needs to maintain enough information to distinguish between bidirectional and unidirectional links to its neighbors. A node may not be able to directly send information to a neighbor if there is no link from the node to the neighbor. Once knowledge of link orientations is available, appropriate routing decisions can be made.

First, let us determine the minimum amount of information participating nodes need to maintain to ensure correctness of the routing protocol. We will concentrate on modifications to protocols like DSDV and AODV to cope with the presence of unidirectional links.

### *5.1. Assumptions*

We model the network as a graph G = (V, E), where V is the set of vertices and E is the set of edges. Some of the edges are assumed to be directed. Every vertex (also referred to as a node) is reachable from every other vertex. Thus, every

[1] DSR [8] does not explicitly assume the presence of only bidirectional links.

[2] Such an assumption may not always be valid in a network with a combination of bidirectional and unidirectional links.

[3] A low mobility network experiences a low frequency of topology changes. Hence, the high overhead route maintenance messages need to be exchanged less frequently.

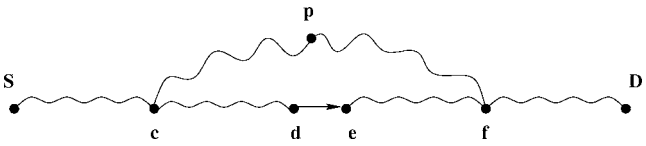


Figure 3. Representation of directed and undirected paths.

node in the network can send packets to every other node in the network.

Let each packet start from the source $x$ with its *Time_To_Live (TTL)* field initialized to *TTL_max*. All nodes have agreed *a priori* on the value of *TTL_max*. Each intermediate node $z$, and the destination $y$ on receiving the packet decrements the TTL field by one. Let us refer to the resultant value as *TTL_receive*. When the packet arrives at the destination node the length of the path traversed by the packet thus far is equal to *TTL_max* − *TTL_recv*. Similarly, every intermediate node, on receiving a packet, can determine the length of the path taken by that packet so far.

*Definitions*

- $path(ab)$: the shortest path from node $a$ to node $b$. As some links are unidirectional, $path(ab)$ may be different from $path(ba)$.
- $path(av_1v_2 \ldots v_kb)$: the shortest path from $a$ to $b$ that passes through vertices $v_i : 1 \leqslant i \leqslant k$ such that $v_i$ precedes $v_j$ if $i < j$.
- $length(path(x))$: number of wireless links in $path(x)$, where $x$ is a sequence of vertices.
- *directed path*$(ab)$: $path(ab)$ is said to be a directed path if it has at least one directed link.

**Lemma 1.** In a network of $n$ nodes, $O(n)$ size distance vector exchange is not sufficient to determine routes in the presence of unidirectional links.

*Proof.* The lemma is proved by contradiction. Let us consider the graph $G$ shown in figure 3. In the figure:

1. $\vec{de}$ is a directed edge.
2. $length(path(cd)) \geqslant 0$.
3. $length(path(ef)) \geqslant 0$.

Let each node $i$ maintain a vector $\mathcal{V}_i$ of length $n$ to be used as the routing table. $\mathcal{V}_i[j].dist$ is node $i$'s knowledge of its path-length to node $j$. Let the shortest path from $c$ to $D$ be the directed path $path(cdefD)$ and let $path(fD)$ be an undirected path. Also, let $path(fpc)$ be a path of length greater than zero between $f$ and $c$. There are two possibilities regarding $path(fpc)$:

*Possibility 1.* It is a directed path from $f$ to $c$. As the distance vectors are exchanged between neighboring nodes, the reachability information about $D$ reaches $c$ along $path(Dfpc)$. Therefore, node $c$'s estimate of the distance to $D$ is $length(path(Dfpc))$, which may be different from $length(path(cdefD))$.

*Possibility 2.* It is an undirected path, or directed from $c$ to $f$. If $path(fpc)$ is directed from $c$ to $f$, node $c$ cannot learn about its distance to $D$ as no path exists from $D$ to $c$. This is a violation of the assumption that every pair of nodes can communicate along a path.

If $path(fpc)$ is undirected, $length(path(fpc))$ must be greater than or equal to $length(path(cdef))$. Otherwise, the shortest path from $c$ to $D$ would have been $path(cpfD)$.

If $length(path(fpc)) > length(path(cdef))$ then due to diffusion of distance vectors from $D$ towards $C$ node $C$'s distance estimate for $D$, i.e., $\mathcal{V}_c[D].dist = length(path(fpc)) + length(path(fD))$. This is greater than the actual path length which is equal to $length(path(cdefD))$. Hence, maintaining only a distance vector will lead to erroneous calculation of path lengths. □

*Basic idea*

Let us once again refer to figure 3 where $path(cdef)$ is the shortest path from $c$ to $f$. Let

$$X = \{x\colon\ x \text{ is a node on } path(cd)\}, \quad \text{and}$$
$$Y = \{y\colon\ y \text{ is a node on } path(ef)\}.$$

As $path(cdef)$ is the shortest path from $c$ to $f$, for all $x$ and $y$, $path(xy)$ goes through vertices $d$ and $e$. As edge $\vec{de}$ is directed, information about $length(path(xy))$ cannot propagate from $y$ to $x$ along the path that goes through $\vec{de}$. However, this information could be conveyed to $x$ if every node $p$ on $path(yfcx)$ propagates $length(path(xy))$, $\forall x \in X,\ y \in Y$. As sets $X$ and $Y$ can be as large as $V$, $|X| = O(n)$ and $|Y| = O(n)$, where $n = |V|$.

Therefore, in the proposed solution node $p$ needs to store and forward $O(n^2)$ units of length information. It may be possible to develop solutions with lower communication overheads. Determination of the lower bound and development of more efficient solutions is the subject of future research.

### 5.2. Data structures and algorithm

It is assumed that each node emits a beacon at regular intervals. A node can hear beacons transmitted by a neighboring node provided the link between them is bidirectional, or directed from the neighbor to itself. The transmission of beacons by different nodes is not synchronized as there is no global clock in the system.

#### 5.2.1. Data structures

Each node $p$ maintains the following data structures:

- $Nodesheard_p$: set of nodes whose beacons have been heard by node $p$ within the last $t$ time units. If $q \in Nodesheard_p$ and $p \in Nodesheard_q$, then there exists a bidirectional link between $p$ and $q$. However, if $q \in Nodesheard_p$ and $p \notin Nodesheard_q$, then there is a unidirectional link from $q$ to $p$. This data structure is modeled after the one by the same name used in the Linked Cluster Algorithm [1,2].
- $D$: an $n \times n$ matrix of 2-tuples, where $n$ is the number of nodes in the network. $D[i, j] = (seq,\ dist)$ means

node $p$ knows that the path from node $i$ to node $j$ is of length *dist*, and the sequence number associated with this information, pertaining to node $j$, is *seq*. Due to the possibility of unidirectional links, $D[i, j].dist$ may not be equal to $D[j, i].dist$. The sequence number associated with a destination is monotonically increasing. Each time node $j$ sends updates to its neighbors, if $j$ knows of a link from $i$ to $j$ then $j$ increases the sequence number associated with the entry $D[i, j]$ by a constant value. As in AODV and DSDV, routing information with a higher sequence number overrides the corresponding information with a smaller sequence number. As a result, stale routing information cannot suppress new routing information. Consequently, knowledge about link disruptions propagates quickly and the *count to infinity* problem (associated with distance vector algorithms) is avoided.

- *To* and *From*: vectors of length $n$, where each entry is a 3-tuple of the form (*seq*, *dist*, *next*) and (*seq*, *dist*, *prev*), respectively. The *To* vector is similar to the distance vector of DSDV as it maintains information about the path length from a node to all other nodes, and the next hop on the path to those nodes. $From_p$ vector contains information about paths from other nodes to $p$. Due to the presence of unidirectional links in the network, and the resultant routing asymmetry, the corresponding *dist* values in the *To* and *From* vectors may be different from each other.

When routing information stabilizes, $To_p$ should have the same *dist* and *seq* values as the corresponding entries in the $p$th row of $D_p$. There should be a similar match between $From_p$ and the $p$th column of $D_p$. This seems to suggest that the $D$ matrix could be modified to add one more field: *prev/next* to each element. The *To* and *From* data structures could be omitted with such a modification. However, this approach is not adopted for the following reasons:

1. There is no point in node $p$ maintaining the information $D_p[i, j].prev$ or $D_p[i, j].next$ where $p \notin \{i, j\}$.
2. Addition of the third field to $D$ will increase the communication overheads when nodes exchange their $D$ matrix with neighbors.

So, the presence of two *seemingly redundant* data structures is actually due to performance considerations.

*Determination of link orientation.* We employ the *Nodesheard* set, in a manner similar to [1], to determine network adjacency. Each node periodically transmits its *Nodesheard* set with its beacon. It also continuously listens for similar transmissions from other nodes. If node $p$ hears that $p \in Nodesheard_q$, node $p$ knows that there exists a bidirectional link between $p$ and $q$. The next time $p$ broadcasts its beacon it includes $q$ in its *Nodesheard* set. When $q$ hears this beacon it, too, knows of the presence of the bidirectional link.

If node $p$ finds that $p \notin Nodesheard_q$, $p$ concludes that there exists a unidirectional link from $q$ to $p$. However, how does $q$ get to know of the presence of this link? For this purpose we employ the matrix $D$, as described next.

*5.2.2. Routing algorithm*

Let $V$ denote the set of nodes in the network. Initially, the $D$ matrix at each node $p$ only contains its adjacency information. Each node periodically transmits its $D$ matrix. The time between successive transmissions of $D$ is a multiple of the time between successive transmissions of the *Nodesheard* set. This is so for two reasons:

1. Transmission of $D$ consumes much more bandwidth than the transmission of *Nodesheard*.
2. Transient noise that may interfere with the reception of a few successive *Nodesheard* messages from a neighbor does not lead a node into erroneously concluding that its path to/from that neighbor is broken.

*On link discovery.* If $p$ discovers a bidirectional link between $p$ and $q$, then $D_p[p, q].dist = D_p[q, p].dist = 1$. If $p$ discovers that there exists a unidirectional link from $q$ to $p$, then $D_p[q, p].dist = 1$. The sequence number associated with each entry is analogous to the sequence number associated with routing table entries in DSDV and AODV with one subtle difference: in the context of unidirectional links they may be associated with the source as opposed to the destination. This difference is explained in the following footnote. The sequence numbers are initialized to zero, and increase with time.

*On receiving D matrix from neighbor.* Let node $p$ receive matrix $D_{\text{recv}}$ from node $q$. If $\overline{pq}$ is a bidirectional link or a unidirectional link from $q$ to $p$, $p$ modifies its $D$ matrix in the following manner on receiving the matrix:

- For all nodes $r \in V$, different from $p$ and $q$:
  - If $D_{\text{recv}}[r, q].seq < D[r, p].seq$ then perform no action using $D_{\text{recv}}[r, q]$.[4]
  - If $((D_{\text{recv}}[r, q].seq == D[r, p].seq)$ OR $((D_{\text{recv}}[r, q].seq > D[r, p].seq)$ AND $(From_p[r] != q))$):
    - $D[r, p].dist = \min(D_{\text{recv}}[r, q].dist + 1, D[r, p].dist)$;
    - if $D[r, p].dist$ has decreased as a result then $From_p[r].prev = q$.
  - If $((D_{\text{recv}}[r, q].seq > D[r, p].seq)$ AND $(From_p[r] == q))$:
    - $D[r, p].dist = D_{\text{recv}}[r, q].dist + 1$.

[4] As opposed to DSDV and AODV, the sequence number comparison is done for entries with the same *source*. So, here the sequence number indicates the age of the reachability information from source to two different, but adjacent destinations. The reason is as follows. Let some link(s) on a path from node $i$ to $j$ be unidirectional. When reachability information with a sequence number tagged by $i$ propagates towards $j$ it indicates the length of the path from $i$ to $j$. Node $j$ cannot use this information to draw inferences about the length of the path from itself to $i$.

- If $D[r, p].dist$ has changed as a result, $D[r, p].seq = From_p[r].seq = D_{\text{recv}}[r, q].seq$.
- If $D_{\text{recv}}[r, q].seq == D[r, q].seq$:
  - $D[r, q].dist = \min(D_{\text{recv}}[r, q].dist, D[r, q].dist)$.
- If $D_{\text{recv}}[r, q].seq > D[r, q].seq$:
  - $D[r, q] = D_{\text{recv}}[r, q]$.

These operations enable node $p$ to determine its distance from other nodes.

- For any arbitrary pair of nodes $r$ and $s$ in $V$, different from $p$ and $q$:
  - If $((D_{\text{recv}}[r, s].seq > D[r, s].seq)$ OR $((D_{\text{recv}}[r, s].seq == D[r, s].seq)$ AND $(D_{\text{recv}}[r, s].dist < D[r, s].dist)))$:
    - $D[r, s] = D_{\text{recv}}[r, s]$.

If link $\overline{pq}$ is a bidirectional link, node $p$ also performs the following operations for all $r \in V$:

I. If $D_{\text{recv}}[q, r].seq < D[p, r].seq$, then do not perform any action using $D_{\text{recv}}[q, r]$.

II. If $D_{\text{recv}}[q, r].seq == D[p, r].seq$:
  - if $D_{\text{recv}}[q, r].dist + 1 < D[p, r].dist$:
    - $To_p[r].dist = D[p, r].dist = D_{\text{recv}}[q, r].dist + 1$,
    - $To_p[r].next = q$;
  - if $D_{\text{recv}}[q, r].seq == D[q, r].seq$:
    - $D[q, r].dist = \min(D_{\text{recv}}[q, r].dist, D[q, r].dist)$;
  - if $D_{\text{recv}}[q, r].seq > D[q, r].seq$:
    - $D[q, r] = D_{\text{recv}}[q, r]$.

III. If $D_{\text{recv}}[q, r].seq > D[p, r].seq$ then:
  - $To_p[r].dist = D[p, r].dist = D_{\text{recv}}[q, r].dist + 1$,
  - $To_p[r].seq = D[p, r].seq = D_{\text{recv}}[q, r].seq$,
  - $To_p[r].next = q$.

The preceding operations are similar to the updates performed by DSDV and AODV. They enable node $p$ to determine its distance to other nodes.

If the received $D$ matrix from node $q$ is such that $D_{\text{recv}}[p, s].dist == 1$ and $s \notin Nodesheard_p$, node $p$ concludes that there exists a unidirectional link from $p$ to $s$. Therefore:

- $To_p[s].dist = D[p, s].dist = 1$,
- $To_p[s].seq = D[p, s].seq = D_{\text{recv}}[p, s].seq$,
- $To_p[s].next = s$.

Also, for every arbitrary node $r$ that is different from $p$ and $s$, $p$ updates its $D$ matrix as follows:

- if $D[p, r].seq$ is equal to $D_{\text{recv}}[s, r].seq$ then updates are performed similar to case II described above, substituting $q$ with $s$;
- if $D_{\text{recv}}[s, r].seq$ is greater than $D[p, r].seq$ then updates are performed similar to case III described above, once again substituting $q$ with $s$.

Thus, each node updates its reachability information and propagates this information to other nodes.

*On detecting link break.* Let $p$'s data structures indicate the existence of a bidirectional link between $p$ and $q$, or a unidirectional link from $q$ to $p$. If $p$ does not hear a certain predetermined number of successive beacons from $q$, then $p$ concludes that direct communication from $q$ to $p$ has been disrupted. Hence, $p$ removes $q$ from $Nodesheard_p$ and performs the following operations:

- increment $From_p[q].seq$ and $D[q, p].seq$,
- $From_p[q].dist = D[q, p].dist = \infty$,
- $From_p[q].prev = \text{NULL}$,
- $\forall r$: $From_p[r].prev == q$:
  - $D[r, p].dist = \infty$,
  - increment $D[r, p].seq$,
- $\forall r$: $To_p[r].next == q$:
  - $D[p, r].dist = \infty$.
- Node $p$ immediately broadcasts its updated $D$ matrix to all its neighbors. The idea is to *propagate bad news fast*.

Let node $p$ be under the impression that it has a unidirectional link to $q$. Let $p$ receive a $D$ matrix from node $s$ such that: $(D_{\text{recv}}[p, q].seq > D[p, q].seq) \wedge (D_{\text{recv}}[p, q].dist == \infty)$. This indicates that the link from $p$ to $q$ has been disrupted. So, $p$ performs the following operations:

- $To_p[q].seq = D[q, p].seq = D_{\text{recv}}[p, q].seq$,
- $To_p[q].dist = D[p, q].dist = \infty$,
- $\forall r$: $To_p[r].next == q$:
  - $D[p, r].dist = \infty$,
  - increment $D[p, r].seq$.
- Node $p$ immediately broadcasts its updated $D$ matrix to all its neighbors.

**Example.** Let us refer back to figure 2. Node $i$ knows that there is a path of length one from $j$ to $i$. This information is forwarded by $i$, through $a$ to the rest of the network. Later, when node $j$ receives $D_{\text{recv}}$ matrix from $k$, $j$ finds that $D_{\text{recv}}[j, i] = 1$. It is at this point that $j$ realizes that it has an outgoing link to $i$. Using this information, along with distance estimates from $i$ to other nodes, $j$ can revise its estimate of its distance to other nodes.

Also, when node $b$ sends its $D$ matrix to node $c$, $c$ realizes that $b$ is two hops away from $i$. Therefore, $c$ concludes that it must be three hops away from $i$.

**Lemma 2.** The algorithm for updating the $D$ matrix and the *To* vector results in loop-free routing.

*Proof.* The proof is by contradiction. Let us assume that prior to an update of the $D$ matrix and the $To$ vector there is no loop. Therefore, $To[r].next$ values form a directed acyclic graph representing acyclic paths of *finite length* from nodes in $V$ to node $r$. Such a directed acyclic graph can be constructed for each *destination* node. Let the following operation result in the formation of a cycle in node $r$'s graph: $To_p[r].next = q$, where nodes $q$ is a neighbor of node $p$. There are two cases when this update to $To_p[r].next$ is performed:

1. Node $p$ gets to know that the sequence number of node $q$'s path to $r$ is greater than the sequence number of its own path to $r$, i.e., $To_p[r].seq < To_q[r].seq$. By construction of the algorithm, node $To_q[r].next$ should have a sequence number that is greater than or equal to $q$'s sequence number. Extending this argument, as the chain of $To[r]$ pointers is traversed, the sequence number must be nondecreasing. As we now have a cycle, the chain should lead back from $q$ to $p$. This means that the $To_p[r].seq$ cannot be less than $To_q[r].seq$: a contradiction.

2. The sequence numbers associated with paths from $p$ and $q$ to $r$ are the same. $To_p[r].next$ is set to $q$ because $D_{\text{recv}}[q, r].dist + 1 < D[p, r].dist$. As this has resulted in a cycle, the path from $q$ to $r$ must lead through $p$. This would imply that $D[p, r].dist < D[q, r].dist$: a contradiction. □

### 5.3. Storage and communication overheads

The storage requirement at each node is $O(n^2)$, where $n$ is the number of nodes in the system. This is significantly greater than distance vector based protocols like DSDV and AODV which only require $O(n)$ units of information to be stored by each mobile node. The increased storage complexity of the proposed scheme is due to the topology matrix $D$ maintained by each node. Similarly, the largest message is of size $O(n^2)$, once again greater than the communication overheads of DSDV and AODV which are $O(n)$.

### 5.4. The sinking feeling

Under some circumstances sink unreachability, as described in section 4, can have an interesting impact on the performance of the proposed routing algorithm. Consider two strongly connected subnetworks $N_1$ and $N_2$.[5] As shown in figure 4, let there be a unidirectional link from node $A \in N_1$ to a node $B \in N_2$. Let there be a path (of one or more links) from $N_2$ to $N_1$ shown by the dotted arc. As a result: (i) information about link $\vec{AB}$ can be diffused to node $A$, (ii) $A$ can propagate this information to other nodes in $N_1$, and (iii) nodes in $N_1$ can route packets to nodes in $N_2$ through the link $\vec{AB}$.

Subsequently, let the path from $N_2$ to $N_1$ be disrupted making the sub-network $N_2$ a *sink* with respect to sub-network $N_1$. Let this be followed by the disappearance of link $\vec{AB}$. Node $B$ senses the disappearance of the link. However, there is no path to propagate this information to $N_1$. If an unreliable MAC sub-layer protocol is being used by $A$ and/or the solution does not enforce the restriction that the directed network be strongly connected all the time then: (i) nodes in $N_1$ will continue to forward packets destined for nodes in $N_2$ to $A$, and (ii) $A$ will keep transmitting them with the impression that they will get to $B$. This is wasteful.

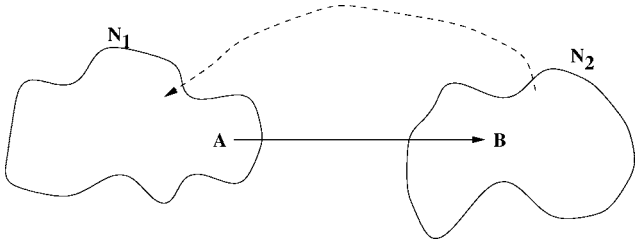


Figure 4. Impact of weakly connected directed graph on routing.

However, as stated in section 5.1, if the protocol requires strong connectivity of the network (every vertex can reach every other vertex along a directed path) for correct operation then the following will happen: the fact that there is no path from $N_2$ to $N_1$ will be propagated among the nodes in $N_1$ in finite time. Consequently, node $A$ will realize that $A$ and $B$ are in different strongly connected components and $A$ will stop communicating messages along $\vec{AB}$. Therefore, a subsequent disappearance of link $\vec{AB}$ will have no further adverse impact on performance.

Hence, routing on unidirectional links has to be considered in conjunction with MAC sub-layer issues. A discussion of such issues in presented in section 6.

### 5.5. Impact of alternative strategy on route stability

A pertinent question to ask at this juncture is: *Is it possible to reduce the storage and communication cost incurred in route maintenance for a network with potentially unidirectional links?*

One possibility could be to ignore all unidirectional links and restrict all operations to bidirectional links. As described in section 4, this can lead to longer routes, or may lead to the impression that the network is partitioned when in reality all node pairs are reachable from each other. Also, links that are bidirectional most of the time may briefly become unidirectional. This may temporarily invalidate some routes. If one were to assume that the link has entirely disappeared for the duration it is unidirectional then this may: (i) invalidate an even greater number of routes for that period, (ii) generate more route update messages.

This will result in reduced *stability* of routes, where stability of a route between a pair of nodes indicates the duration for which the route remains unchanged. *It is to be noted that protocols like AODV and DSR cache routing information to reduce the overhead of route discovery. Reduced route stability will result in reduced effectiveness of caching, and shorter cache invalidation time.*

[5] A directed graph is said to be strongly connected if there exist directed paths from every node to every other node.

If link unidirectionality is a rare phenomenon and its impact on route length and stability is small, one could ignore all unidirectional links and only incur $O(n)$ storage and communication overheads. The reduction in overheads from $O(n^2)$ to $O(n)$ throughout the lifetime of the network may be more desirable than occasional increase in path lengths and reduction in route stability. However, an implementer should make the decision as to whether link unidirectionality needs to be considered or ignored only after careful interference modeling and extensive simulation experiments.

The observation that adjacent nodes need to exchange more than $O(n)$ information raises an interesting question. Link-state routing algorithms require a total of $O(n^2)$ information, i.e., entire network topology to be conveyed to each router. The proposed algorithm, which started out as a modification of DSDV, also requires $O(n^2)$ information to be sent along each incident edge of a node. So, in the presence of unidirectional links would it be prudent to concentrate on link-state routing algorithms. Further study is required before making any assertion about the superiority of one routing algorithm over the other in the ad hoc network scenario.

The presence of unidirectional links may also affect hierarchical routing algorithms. Unidirectional links may result in routing asymetry between cluster-heads. So, the $m$ cluster-head ($m \leqslant n$) may have to exchange $O(m^2)$ information to maintain routes if the algorithm described in this paper is employed. However, once again, further investigation is required before reaching a conclusion.

## 6. MAC sub-layer issues for unidirectional links

Various wireless MAC sub-layer protocols, including IEEE 802.11, require the receiver to send an acknowledgement (or a NACK) to the sender. This assumes bidirectional communication between the sender and the receiver. However, if a node sends packets to another node along a unidirectional link the receiver cannot send MAC sub-layer acknowledgements along the same link. Instead, the acknowledgements have to be *routed* to the sender.

Routing MAC sub-layer acknowledgements mixes the network and data link layer issues. If a path exists from the receiver to the sender one possible solution could be to *tunnel* the MAC sub-layer acknowledgements as a network layer packet much the same way the UniDirectional Link Routing (UDLR) Working Group of the IETF has suggested for networks involving satellite links and/or cable connections [7]. Tunneling acknowledgements would require the designer to consider its impact on performance. As the acknowledgements have to traverse a multi-hop path the latency of MAC sub-layer communication is increased. So, the node sending data along a unidirectional link would need to maintain bigger MAC sub-layer windows (if a sliding window protocol is being used) to sustain a steady flow of data along the link. The increased latency at the MAC sub-layer could also impact the upper layers of the protocol stack. One possible example at the transport layer could be the impact on TCP timers and throughput.

If for a unidirectional link from $A$ to $B$ a reverse path from $B$ (receiver) to $A$ (sender) does not exist $B$ cannot tunnel acknowledgements to $A$. In such a situation if $A$ wishes to continue using the link $\vec{AB}$ to route packets $A$ has to use an unreliable MAC sub-layer protocol, i.e., one that does not expect acknowledgements and cannot do any flow control using sliding windows. *A reliable MAC sub-layer protocol can be used in conjunction with unidirectional links only if the network is strongly connected.*

## 7. Conclusion and future work

Most of the research in mobile computing tends to assume that all links are bidirectional. However, due to a variety of reasons, only unidirectional communication may be possible between some pairs of adjacent nodes. Existing distance vector based algorithms will fail in the presence of such links.

We described the adverse impact of unidirectional links on existing distance vector based routing algorithms. We showed that diffusing distance vectors with one component per node is not enough. We also described simple data structures and proposed a strategy to propagate routing information in networks with a combination of unidirectional and bidirectional links. The proposed strategy is a modification of DSDV and AODV: well known routing algorithms proposed for wireless ad hoc networks. It incurs higher communication and storage overheads of $O(n^2)$.

We intend to work on efficient storage and information propagation strategies to reduce the absolute size of messages exchanged between neighboring nodes. This is of significance due to the low bandwidth of wireless links. Also, the $O(n^2)$ size of route dissemination messages points towards the need to evaluate link-state routing strategies for networks with unidirectional links. In the future we intend to investigate the impact of unidirectional links on hierarchical routing algorithms. We will also try to gain a better understanding of the role of sink nodes in a network, and the role of MAC sub-layer protocols in networks with unidirectional links.

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