## Switching



Function: connect inputs to outputs, so that bits or packets that arrive on one link, leave on another designated link.

## Performance measures:

- Delay: per packet (ps), per bit (cs)
- Set-up time: per circuit (cs or virtual cs)
- Throuhgput: \# lines, rates
- Complexity: \# crosspoints (cs), buffer size (ps)


## Examples:

a) $\mathrm{N} \times \mathrm{N}$ point - to - point switch:

We want to be able to connect any input to any output, as long as two different inputs do not have the same output

\# different configurations = N!
\# crosspoints $\geq \log _{2}(\mathrm{~N}!)=\Theta(\mathrm{NlogN})$
b) $\mathrm{N} \times \mathrm{M}$ multipoint switch

We want to be able to connect any input to any set of outputs, but no two inputs should be connected to the same output.

## Clos Networks

Specified by (IN, $\mathrm{N}_{1}, \mathrm{~N}_{2}, \mathrm{~N}_{3}$, OUT)
$6 \times 8$ switch


- = elementary cross-bar switch

A switch is non-blocking if all the one-to-one connections are compatible.

A switch is strictly non-blocking (SNB) if any new connection from a free input to free output is possible without modifying other connections.

Otherwise, it is rearrangeably non-blocking (RNB).

Theorem: if $\mathrm{N}_{2} \geq I N+O U T-1$, the Clos switch is SNB.


## Proof:

Assume we want to set-up a connection from $a$ to $b$.
a connected to $\leq \mathrm{IN}-1$ middle switches
b connected to $\leq$ OUT-1 middle switches
$\Rightarrow$ there is a middle switch available.

Theorem: if $\mathrm{N}_{2} \geq \max \{\mathrm{IN}, \mathrm{OUT}\}$, the Clos switch is RNB.


## Complexity of a Clos switch (example)


$N=p q \Rightarrow$ crossbar requires $p^{2} q^{2}$ crosspoints
RNB Clos: $\mathrm{N}_{2}=\mathrm{p}$
Assume each • is implemented as a crossbar.
\# crosspoints $=q p^{2}+p q^{2}+q p^{2}=p^{2} q^{2}(1 / p+2 / q)<p^{2} q^{2}$
SNB Clos: $N_{2}=2 p-1$
\# crosspoints $=2 p q(2 p-1)+(2 p-1) q^{2}=$
$=4 p^{2} q+2 p q^{2}-2 p q-q^{2}=$
$=p^{2} q^{2}\left(4 / q+2 / p-2 / p q-1 / q^{2}\right)$
e.g. if $p=q=100$, SNB has only $6 \%$ of the crosspoints of a crossbar.

## Benes Network (Rearrangeably nonblocking)

Let $\mathrm{N}=2^{\mathrm{n}}$ and consider the recursive construction:


Looks like a (2, N/2, 2, N/2, 2) Clos network
$\mathrm{N}_{2}=2 \geq \max \{\mathrm{IN}, \mathrm{OUT}\}=\max \{2,2\} \Rightarrow \mathrm{RNB}$
(provided that the
$\mathrm{N} / 2 \times \mathrm{N} / 2$ boxes
are RNB)

Each $\mathrm{N} / 2 \times \mathrm{N} / 2$ is itself constructed recursively as a Benes network

Each N/ $2 \times \mathrm{N} / 2$ switch can again be decomposed

$\mathrm{T}(\mathrm{N})$ : \# of $2 \times 2$ switches in $\mathrm{N} \times \mathrm{N}$ Benes

$$
\left.\begin{array}{c}
T(N)=N+2 T(N / 2) \\
T(2)=1
\end{array}\right\} \Rightarrow T(N)=\left(2 \log _{2} N-1\right) \frac{N}{2}
$$

A $2 \times 2$ switch requires 4 cross points: $\bullet \Rightarrow$
$\Rightarrow 4 \mathrm{Nlog}_{2} \mathrm{~N}-2 \mathrm{~N}$ crosspoints $=$ optimal order
Example: $\mathrm{N}=10^{4} \Rightarrow 5 \cdot 10^{5}$ as opposed to $10^{8}$ required by a crossbar

## Routing in a Benes Network

Start idle. Let C be a desired set of connections.


Step 1: Select input not yet selected. (Terminate if none exists)

Step 2: Connect input to desired output (of S, say) via U

Step 3: If other output of $S$ desires connections to input of $T$ (say), connect via $L$ Go to step 1.

Apply the algorithm recursively to U and L

## Fast Packet Switching (FPS)

The frequency of changes in the switch configuration is orders of magnitude greater in the case of packet switching than in circuit switching ( $\mu \mathrm{s}$, or even ns, as opposed to seconds)


Tag $=\left\{\begin{array}{l}\text { destination address (datagram) } \\ \text { virtual circuit identifier (VC switching) }\end{array}\right.$

Advantage of FPS: flexible bandwidth allocation
Disadvantage of FPS: buffering is needed

## Time Division Switching (e.g. telephone network)



Delay $\leq \mathbf{2 N}$ slots

Disadvantage: internal rate is N times larger

## Basic Designs

Shared buffer Distributed buffer Output buffer

## Shared Buffer

One linked list per output. One linked list of free buffer.


Buffer

Advantage: maximum utilization of buffers.
Disadvantage: fast pointer manipulation needed.

## Output Buffers



Advantage: Conceptually simple
Disadvantage: Requires fast bus

## Distributed Buffer


(other examples are Baseline, Flip, Delta, etc)

## Self-routing in Omega (others are similar)



Here the tag is the output port number.
In the $\mathrm{i}^{\text {th }}$ stage, if corresponding $\left(\mathrm{i}^{\text {th }}\right)$ bit of tag is 1 it goes down and if it is 0 it goes up.

